

Randomized Quick sort

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Instead of always using $A[r]$ as the pivot, using random sampling, we will use a randomly chosen element from subarray $A[p..r]$.

Because the pivot element is randomly chosen, we expect the split of the input array to be reasonably well balanced on average.

The worst case running time for randomized Quick-sort is $\Theta(n \log n)$.

RANDOMIZED-PARTITION (A, p, r)

1. $i \leftarrow \text{RANDOM}(p, r)$
2. exchange $A[i] \leftrightarrow A[r]$
3. return PARTITION(A, p, r)

PARTITION(A, p, r)

1. $x \leftarrow A[r]$
2. $i \leftarrow p - 1$
3. for $j \leftarrow p$ to $r - 1$
4. {if $x \geq A[j]$
5. { $i = i + 1$
6. exchange $A[i] \leftrightarrow A[j]$
7. } }
8. exchange $A[i + 1] \leftrightarrow A[r]$
9. return $i + 1$

RANDOMIZED-QUICKSORT(A, p, r)

1. if ($p < r$)
2. { $q \leftarrow \text{RANDOMIZED-PARTITION}(A, p, r)$
3. RANDOMIZED-QUICKSORT($A, p, q - 1$)
4. RANDOMIZED-QUICKSORT($A, q + 1, r$)
5. }